

## SC9: Quantitative chemistry

### Lesson sequence

1. Formula masses
2. Calculating empirical formulae
3. Conservation of mass
4. Calculating reacting masses
5. Moles (HT)
6. Stoichiometry of reactions (HT)

### 1. Formula masses

|   |   |
|---|---|
| <b>Molecular formula</b>                          | Gives the number of atoms of each element present in a molecule.  |
| <b>Empirical formula</b>                          | Gives the number of atoms of each element present in a compound as the simplest whole number ratio.                                   |
| <b>Converting molecular to empirical formulae</b> | Divide the number of each atom by the highest common factor of all of the atoms.  |
| <b>Molecular to empirical formula examples</b>    | $C_2H_4 \rightarrow CH_2$ (divided by 2)<br>$C_6H_{12}O_6 \rightarrow CH_2O$ (divided by 6)<br>$H_2O \rightarrow H_2O$ (divided by 1) |
| <b>Relative atomic mass, <math>A_r</math></b>     | The mass of an atom relative to $1/12^{th}$ the mass of carbon-12. No units.  |
| <b>Relative formula mass, <math>M_r</math></b>    | The mass of one unit of a formula, found by adding the relative atomic masses of all of the atoms in it.                              |

### Worked examples W1

Calculate the  $M_r$  of carbon dioxide ( $CO_2$ ).

$$= A_r(C) + (2 \times A_r(O))$$

$$= 12 + (2 \times 16)$$

So,  $M_r$  of  $CO_2 = 44$

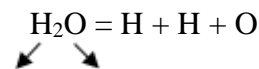
### Relative Formula Mass – RFM

The Relative Formula Mass ( $M_r$ ) of a compound is the sum of the relative atomic masses of all its elements added together.

In order to calculate the RFM of a compound you must know the formula and the  $A_r$ 's of each of the atoms involved ( $H = 1$ ,  $O = 16$ ).

Example: Find the  $M_r$  of water,  $H_2O$

Step 1: Write the formula



Step 2: Substitute the  $A_r$ 's

$$1 + 1 + 16$$

Step 3: Add them up to get the  $M_r$

$$1 + 1 + 16 = 18$$

|                         |                     |                      |                       |                         |                        |                        |
|-------------------------|---------------------|----------------------|-----------------------|-------------------------|------------------------|------------------------|
| $H = 1$<br>Hydrogen     | $C = 12$<br>Carbon  | $N = 14$<br>Nitrogen | $O = 16$<br>Oxygen    | $Na = 23$<br>Sodium     | $Mg = 24$<br>Magnesium | $Al = 27$<br>Aluminium |
| $P = 31$<br>Phosphorous | $S = 32$<br>Sulphur | $Fe = 56$<br>Iron    | $Cu = 63.5$<br>Copper | $Cl = 35.5$<br>Chlorine | $Ca = 40$<br>Calcium   |                        |

Using the method shown and the  $A_r$ 's above calculate the  $M_r$ 's for the following:

|                                |                              |                                    |                                |
|--------------------------------|------------------------------|------------------------------------|--------------------------------|
| Sodium chloride – NaCl         | Methane – $CH_4$             | Sodium hydroxide – NaOH            | Aluminium oxide – $Al_2O_3$    |
| .....                          | .....                        | .....                              | .....                          |
| .....                          | .....                        | .....                              | .....                          |
| .....                          | .....                        | .....                              | .....                          |
| Copper sulphate – $CuSO_4$     | Ethane – $C_2H_6$            | Ethene – $C_2H_4$                  | Calcium hydroxide – $Ca(OH)_2$ |
| .....                          | .....                        | .....                              | .....                          |
| .....                          | .....                        | .....                              | .....                          |
| .....                          | .....                        | .....                              | .....                          |
| Iron sulphate – $Fe_2(SO_4)_3$ | Ammonium chloride – $NH_4Cl$ | Ammonium sulphate – $(NH_4)_2SO_4$ |                                |
| .....                          | .....                        | .....                              |                                |
| .....                          | .....                        | .....                              |                                |
| .....                          | .....                        | .....                              |                                |



### 3. Conservation of mass

|  |  |
|--|--|
| <b>Conservation of mass</b>                    | The total mass of products must equal the total mass of reactants.   |
| <b>Precipitation reaction</b>                  | A reaction that produces a solid precipitate by mixing two solutions.  |
| <b>Closed system</b>                           | A system in which no chemicals can enter or leave, such as a sealed test tube.   |
| <b>Open system</b>                             | A system in which chemicals can enter or leave – such as an open test tube.  |
| <b>Conservation of mass in a closed system</b> | No atoms are able to enter or leave, so the total mass stays the same – for example a precipitation reaction in a closed flask.  |
| <b>Conservation of mass in an open system</b>  | For example, a carbonate reacting with acid producing CO <sub>2</sub> bubbles: the mass appears to decrease because you can't weigh the gas that goes into the air, however it is still there. |

### 3. Concentration

|   |  |
|---|--|
| <b>Concentration</b>                                | The amount of a solute dissolved in a certain volume of solvent.   |
| <b>Calculating concentration (g/dm<sup>3</sup>)</b> | $\frac{\text{Mass of solute (g)}}{\text{Volume of solution (dm}^3\text{)}}$  |
| <b>Decimetre (dm<sup>3</sup>)</b>                   | A unit of volume equivalent to 1000cm <sup>3</sup> , to convert from cm <sup>3</sup> to dm <sup>3</sup> divide the volume by 1000. |

To work out concentrations you need to know the following formula:

$$\text{Concentration (mol dm}^{-3}\text{)} = \frac{\text{mass (g)}}{\text{volume of solution (dm}^{-3}\text{)}}$$

You also need to know that 1 dm<sup>3</sup> = 1000cm<sup>3</sup>, which means that to convert to cm<sup>3</sup> to dm<sup>3</sup> you should divide by 1000.

Work out the concentrations (in g/dm<sup>3</sup>) of the following solutions:

1. 20g of NH<sub>3</sub> in 500cm<sup>3</sup>

.....

.....

2. 10g of Br<sub>2</sub> in 2000cm<sup>3</sup>

.....

.....

3. 18g of NaOH on 300cm<sup>3</sup>

.....

.....

Work out the mass of the solute in the following solutions

4. 250cm<sup>3</sup> of a 200g/dm<sup>3</sup> solution of Ca(OH)<sub>2</sub>

.....

.....

5. 50cm<sup>3</sup> of a 0.5 M solution of HNO<sub>3</sub>

.....

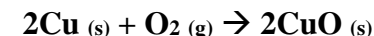
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Use the balanced equations to answer the following questions.

- 1) 12.4g of copper carbonate was heated and formed 8.0g of copper oxide. Calculate the mass of carbon dioxide produced.



- 2) 1.27g of copper was heated in air and formed 1.59g of copper oxide. Calculate the mass of oxygen that reacted with the copper.



lead nitrate solution

potassium iodide solution



yellow precipitate of lead iodide in a colourless solution of potassium nitrate

empty flask

**B** The total mass of the reactants always equals the total mass of products.

## 4. Calculating reacting masses

|                                    |   |
|------------------------------------|---|
| <b>Excess reactant</b>             | Any reactant which is not used up completely in a reaction because there is more of it than needed.   |
| <b>Limiting reactant</b>           | Any reactant of which is completely used up in a reaction. The limiting reactant determines how much product is made.   |
| <b>Calculating reacting masses</b> | <ul style="list-style-type: none"> <li>- Write out the balanced equation</li> <li>- Write the mass of the chemical you are given, and 'm' for the mass you are finding under their symbols</li> <li>- Draw a line underneath the masses to make it a division</li> <li>- Calculate the <math>M_r</math> of each, multiply by the big numbers and write under the line.</li> <li>- Put an equals sign between the two to form an equation.</li> <li>- Solve for 'm'</li> </ul> |

### Calculating the mass of a product

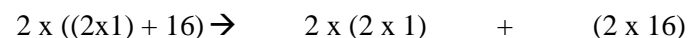
Sometimes, we need to be able to work out how much of a substance is produced in a chemical reaction.

Example: What mass of hydrogen is produced by the electrolysis of 4g of water?

Step 1: Write down the balanced equation, and underline the substances mentioned in the question:



Step 2: Work out the relative formula mass ( $M_r$ ) of each substance:



Step 3: Since the question only mentions water and hydrogen, you can ignore the oxygen. You just need the ratio of mass of  $\text{H}_2\text{O}$  to mass of  $\text{H}_2$ :

So, 36g of water produces 4g of hydrogen.

1g of water produces  $(4 \div 36)$  g of hydrogen (Divide both sides by 36)

4g of water produces  $(4 \div 36) \times 4$  g of hydrogen

$$= 0.44\text{g of hydrogen}$$

### Worked example

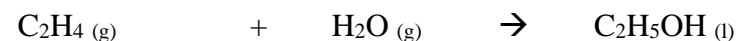
Calculate the mass of chlorine needed to make 53.4g of aluminium chloride.

|   |  |
|---|--|
| Write the balanced equation   | $2\text{Al} + 3\text{Cl}_2 \rightarrow 2\text{AlCl}_3$   |
| Calculate relative formula masses of the substances needed  | $M_r \text{Cl}_2 = 2 \times 35.5 = 71$<br>$M_r \text{AlCl}_3 = 27 + (3 \times 35.5) = 133.5$                                   |
| Calculate ratio of masses (multiply $M_r$ values by the balancing numbers shown in the equation).                           | $3\text{Cl}_2$ makes $2\text{AlCl}_3$<br>so $3 \times 71 = 213$ g $\text{Cl}_2$ makes $2 \times 133.5 = 267$ g $\text{AlCl}_3$ |
| Work out the mass for 1 g of reactant or product. (Here we want 1 g of the product because that's the mass we know already) | $\frac{213}{267}$ g $\text{Cl}_2$ makes $\frac{267}{267}$ g $\text{AlCl}_3$  |
| Scale up or down (from 1 g to the mass you are given)   | $0.798$ g $\text{Cl}_2$ makes $1$ g $\text{AlCl}_3$<br>$42.6$ g $\text{Cl}_2$ makes $53.4$ g $\text{AlCl}_3$                   |

Q1) What mass of aluminium is produced from 100 tonnes of aluminium oxide? (Al = 27, O = 16)



Q2) What mass of ethanol ( $\text{C}_2\text{H}_5\text{OH}$ ) is produced from the reaction of 14 tonnes of ethane ( $\text{C}_2\text{H}_4$ )? (C = 12, H = 1, O = 16)



## 5. Moles (HT)

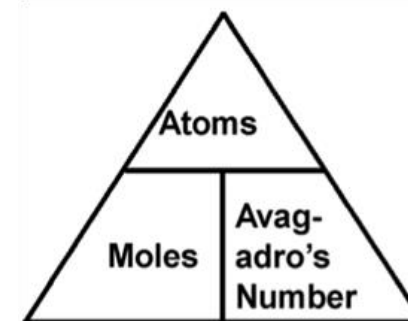
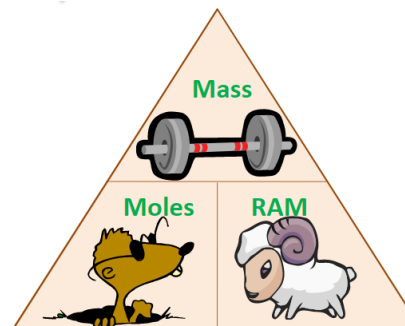
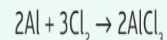
|   |   |
|---|---|
| <b>Moles</b>  | The unit of measurement of chemicals – one mole of any chemical is the same amount.                           |
| <b>One mole</b>   | An amount of a chemical such that one mole has a mass in grams that is the same as its relative formula mass. |
| <b>Avogadro's constant</b>  | $6.02 \times 10^{23}$ : the number of atoms/molecules present in one mole of a substance.                     |
| <b>Calculating moles from mass</b>                                  | Quantity in moles = mass / relative formula mass  |
| <b>Calculating moles from a number of particles</b>                 | Quantity in moles = number of particles / $6.02 \times 10^{23}$   |
| <b>Calculating the number of particles from a mass of substance</b> | Number of particles = (mass / relative formula mass) $\times 6.02 \times 10^{23}$                             |

### Worked example W2

10.8g of aluminium reacted with 42.6g of chlorine,  $\text{Cl}_2$ , to produce aluminium chloride,  $\text{AlCl}_3$ . Deduce the balanced equation for the reaction.

|  | Al                      | $\text{Cl}_2$                      |
|--|-------------------------|------------------------------------|
| Calculate the number of moles<br>(= mass/ $A_r$ or $M_r$ ) | $\frac{10.8}{27} = 0.4$ | $\frac{42.6}{2 \times 35.5} = 0.6$ |
| Divide by the smaller                                      | $\frac{0.4}{0.4} = 1$   | $\frac{0.6}{0.4} = 1.5$            |
| Simplest whole number ratio                                | $1 \times 2 = 2$        | $1.5 \times 2 = 3$                 |

So 2 mol of Al react with 3 mol of  $\text{Cl}_2$ . The equation is completed by adding the formula of the product and balancing in the normal way.



Avagadro's constant =  $6.02 \times 10^{23}$

- 1 Calculate the number of molecules in 0.5 mol of carbon dioxide,  $\text{CO}_2$

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 .....

Calculate the number of molecules in 2 mol of oxygen,  $\text{O}_2$ .

.....  
 .....

- 2 Calculate the number of moles in  $1.505 \times 10^{23}$  atoms of sodium

.....  
 .....

Calculate the number of molecules in  $1.806 \times 10^{24}$  atoms of copper.

.....  
 .....

- 3 Calculate the number of molecules in 9 g of hydrogen,  $\text{H}_2$

.....  
 .....

Calculate the number of molecules in 48 g of oxygen,  $\text{O}_2$ .

.....  
 .....

- 1 Calculate the number of **moles** of water molecules,  $\text{H}_2\text{O}$ , in 9 g of water

.....  
 .....

Calculate the number of **moles** of ethanol molecules,  $\text{C}_2\text{H}_5\text{OH}$ , in 9.2 g of ethanol.

.....  
 .....

- 2 Calculate the mass of 2.5 mol of potassium iodide, KI

.....  
 .....

Calculate the mass of 0.125 mol of calcium sulfate,  $\text{CaSO}_4$ .

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 .....

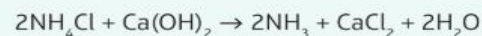


### 6. Stoichiometry (HT)

|                                   |  |
|-----------------------------------|--|
| <b>Stoichiometry</b>              | The ratio of the number of moles of each substance involved in a reaction.   |
| <b>Stoichiometric coefficient</b> | The 'big' numbers written in a balanced equation.  |
| <b>Deducing stoichiometry</b>     | <ul style="list-style-type: none"> <li>- Calculate the number of moles present of each of the reactants (or products)</li> <li>- Find the simplest whole-number ratio</li> <li>- Balance in the normal way to find the numbers of products (or reactants)</li> </ul> |

### Worked example W1

1.50 g of ammonium chloride and 4.00 g of calcium hydroxide are heated together to form ammonia.

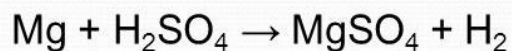


- a** Which is the limiting reactant?
- b** Calculate the mass of ammonia formed.
- a** The equation shows that 2 mol of  $\text{NH}_4\text{Cl}$  reacts with 1 mol of  $\text{Ca}(\text{OH})_2$   
 number of moles of  $\text{Ca}(\text{OH})_2 = 4.00 \text{ g} / (40 + 2(16 + 1)) = 0.0541 \text{ mol}$   
 We need:  $2 \times 0.0541 = 0.108 \text{ mol NH}_4\text{Cl}$  to react with 0.0541 mol of  $\text{Ca}(\text{OH})_2$ .  
 We have:  $1.50 \text{ g} / (14 + (4 \times 1) + 35.5) = 0.0280 \text{ mol}$   
 We have less than the 0.0541 mol of  $\text{NH}_4\text{Cl}$  needed;  $\text{NH}_4\text{Cl}$  = limiting reactant.

- b** The equation shows that the number of moles of  $\text{NH}_3$  made equals the number of moles of  $\text{NH}_4\text{Cl}$  used.

So, 0.0280 mol of  $\text{NH}_4\text{Cl}$  forms 0.0280 mol of  $\text{NH}_3$

mass of  $\text{NH}_3$  formed = mol  $\times M_r = 0.0280 \times (14 + (3 \times 1)) = 0.476 \text{ g}$



- Identify the stoichiometric ratio between magnesium and sulphuric acid in the reaction above.  
.....
- If 5 moles of magnesium is reacted with 7 moles of sulphuric acid, which reagent is in excess?  
How many moles of each product is formed?  
.....  
.....



- Identify the stoichiometric ratio between iron oxide and carbon monoxide in the reaction above.  
.....
- If 480 tonnes of iron oxide is reacted with 308 tonnes of carbon monoxide, which reagent is in excess? How many moles of each product is formed?  
.....  
.....

- 2.76 g sodium reacts with 5.70 g titanium chloride,  $\text{TiCl}_4$  to form titanium and sodium chloride,  $\text{NaCl}$ . Use this data to deduce the balanced equation for the reaction.

Relative atomic masses:

Na = 23    Cl = 35.5    Ti = 48

.....  
 .....  
 .....

- $\text{TiCl}_4 + 2\text{Mg} \rightarrow \text{Ti} + 2\text{MgCl}_2$

What mass of Titanium (Ti) can be made when 1.9g of Titanium chloride ( $\text{TiCl}_4$ ) reacts with 6g of magnesium (Mg)?

.....  
 .....  
 .....

- $\text{WO}_3 (\text{s}) + 3\text{H}_2 (\text{g}) \rightarrow \text{W} (\text{s}) + 3\text{H}_2\text{O} (\text{l})$

What mass of Tungsten (W) can be made when 23.2g of Tungsten oxide ( $\text{WO}_3$ ) reacts with 20g of hydrogen ( $\text{H}_2$ )?

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 .....  
 .....