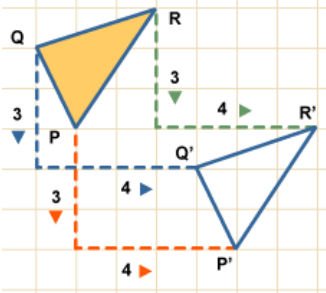
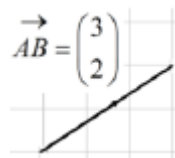
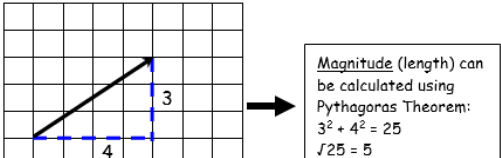

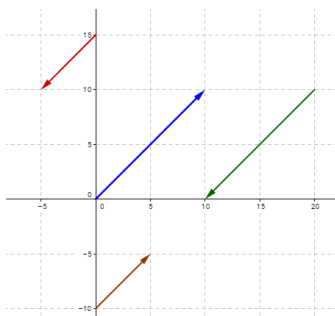
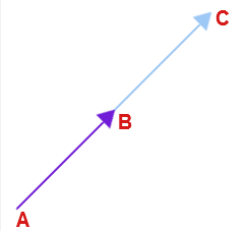
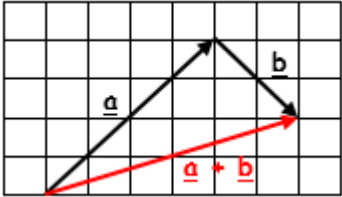
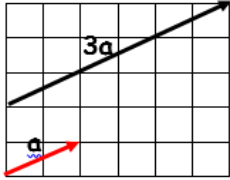
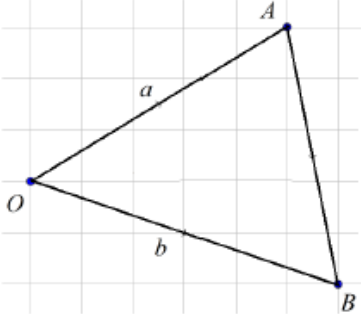
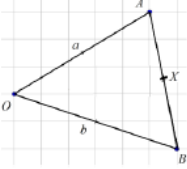


## Topic: Vectors

Topic/Skill	Definition/Tips	Example
1. Translation	<p><b>Translate</b> means to <b>move a shape</b>. The shape does not change <b>size</b> or <b>orientation</b>.</p>	
2. Vector Notation	<p>A vector can be written in 3 ways:</p> $\mathbf{a} \quad \text{or} \quad \overrightarrow{AB} \quad \text{or} \quad \begin{pmatrix} 1 \\ 3 \end{pmatrix}$	
3. Column Vector	<p>In a column vector, the <b>top</b> number moves <b>left (-) or right (+)</b> and the <b>bottom</b> number moves <b>up (+) or down (-)</b></p>	<p><math>\begin{pmatrix} 2 \\ 3 \end{pmatrix}</math> means '2 right, 3 up'</p> <p><math>\begin{pmatrix} -1 \\ -5 \end{pmatrix}</math> means '1 left, 5 down'</p>
4. Vector	<p>A <b>vector</b> is a quantity represented by an arrow with both <b>direction</b> and <b>magnitude</b>.</p> $\overrightarrow{AB} = -\overrightarrow{BA}$	
5. Magnitude	<p>Magnitude is defined as the <b>length</b> of a vector.</p>	
6. Equal Vectors	<p>If two vectors have the <b>same magnitude and direction</b>, they are <b>equal</b>.</p>	
7. Parallel Vectors	<p><b>Parallel</b> vectors are <b>multiples</b> of each other.</p>	<p><math>2\mathbf{a} + \mathbf{b}</math> and <math>4\mathbf{a} + 2\mathbf{b}</math> are parallel as they are multiple of each other.</p> 

8. Collinear Vectors	<p><b>Collinear</b> vectors are vectors that are on the <b>same line</b>.</p> <p>To show that two vectors are <b>collinear</b>, show that one vector is a <b>multiple</b> of the other (parallel) <b>AND</b> that both vectors <b>share a point</b>.</p>	
9. Resultant Vector	<p>The <b>resultant</b> vector is the vector that results from <b>adding</b> two or more vectors together.</p> <p>The resultant can also be shown by <b>lining up</b> the <b>head</b> of one vector with the <b>tail</b> of the other.</p>	<p>if <math>\underline{a} = \begin{pmatrix} 4 \\ 4 \end{pmatrix}</math> and <math>\underline{b} = \begin{pmatrix} 2 \\ -2 \end{pmatrix}</math></p> <p>then <math>\underline{a} + \underline{b} = \begin{pmatrix} 4 \\ 4 \end{pmatrix} + \begin{pmatrix} 2 \\ -2 \end{pmatrix} = \begin{pmatrix} 6 \\ 2 \end{pmatrix}</math></p> 
10. Scalar of a Vector	<p>A <b>scalar</b> is the <b>number</b> we <b>multiply</b> a vector by.</p>	 <p>Example:  <math>3\mathbf{a} + 2\mathbf{b} =</math>  <math>= 3\begin{pmatrix} 2 \\ 1 \end{pmatrix} + 2\begin{pmatrix} 4 \\ -1 \end{pmatrix}</math>  <math>= \begin{pmatrix} 6 \\ 3 \end{pmatrix} + \begin{pmatrix} 8 \\ -2 \end{pmatrix}</math>  <math>= \begin{pmatrix} 14 \\ 1 \end{pmatrix}</math></p>
11. Vector Geometry	 <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <math display="block">\begin{matrix} \vec{OA} = a &amp; \vec{AO} = -a \\ \vec{OB} = b &amp; \vec{BO} = -b \end{matrix}</math> </div> <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <math display="block">\begin{matrix} \vec{AB} = \vec{AO} + \vec{OB} = -a + b = b - a \\ \vec{BA} = \vec{BO} + \vec{OA} = -b + a = a - b \end{matrix}</math> </div>	<p><b>Example 1:</b> <math>X</math> is the midpoint of <math>AB</math>. Find <math>\vec{OX}</math></p> <p><b>Answer:</b> Draw <math>X</math> on the original diagram</p>  <p>Now build up a journey.  You could use <math>\vec{OX} = \vec{OA} + \frac{1}{2}\vec{AB}</math>.</p> <p>This will give: <math>\vec{OX} = a + \frac{1}{2}(b - a)</math>.</p> <p>This will simplify to <math>\frac{1}{2}a + \frac{1}{2}b</math> or <math>\frac{1}{2}(a + b)</math></p>